

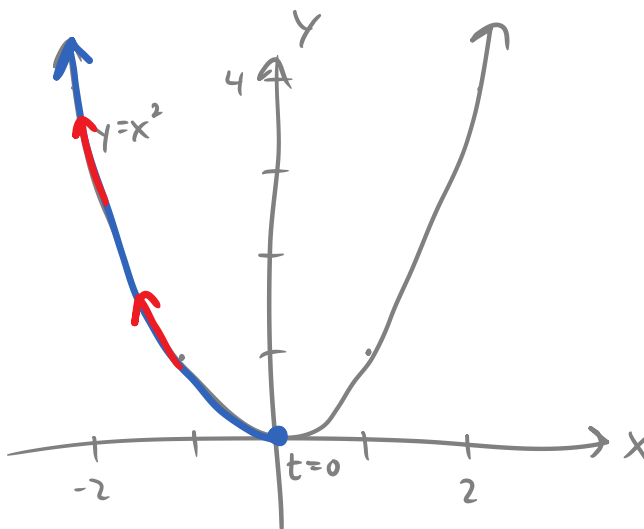
1. Given the following parametric equations/intervals of a particle in the  $xy$ -plane, find the related Cartesian equation and graph it. Then, indicate the portion of the graph traced by the particle and the direction of motion.

$$x = -\sqrt{t}, \quad y = t, \quad t \geq 0$$

$$x = -\sqrt{y}$$

$$\boxed{y = x^2}$$

↑  
parabola



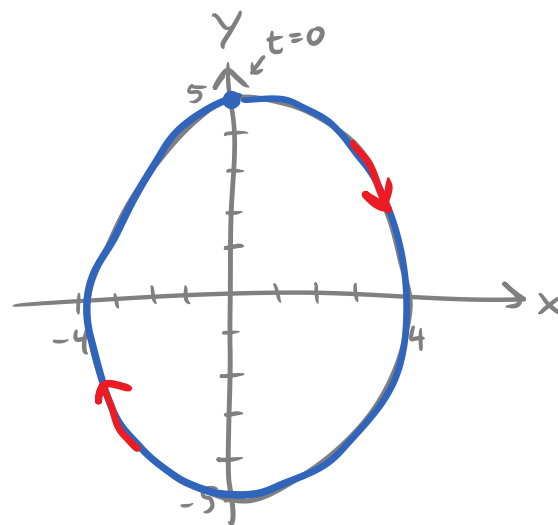
2. Given the following parametric equations/intervals of a particle in the  $xy$ -plane, find the related Cartesian equation and graph it. Then, indicate the portion of the graph traced by the particle and the direction of motion.

$$x = 4 \sin t, \quad y = 5 \cos t, \quad 0 \leq t \leq 2\pi$$

$$\sin t = \frac{x}{4}, \quad \cos t = \frac{y}{5}$$

$$\sin^2 t + \cos^2 t = 1$$

$$\boxed{\frac{x^2}{16} + \frac{y^2}{25} = 1} \leftarrow \text{Ellipse}$$



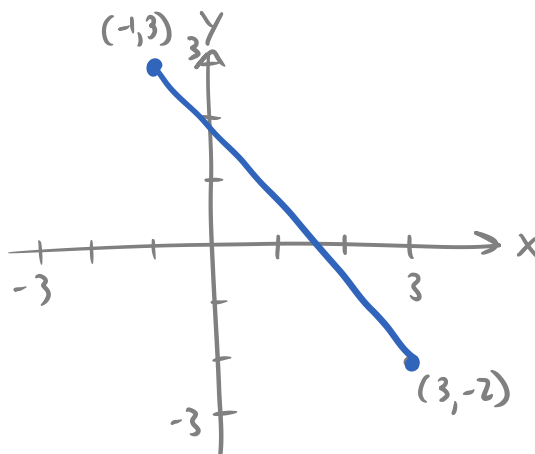
3. Find a parametrization for the line segment with endpoints  $(-1, 3)$  and  $(3, -2)$ .

$$x = -1 + \overbrace{(3 - (-1))}^{\Delta x} t$$

$$= -1 + 4t$$

$$y = 3 + \overbrace{(-2 - 3)}^{\Delta y} t$$

$$= 3 - 5t$$



$$x = -1 + 4t, \quad y = 3 - 5t, \quad 0 \leq t \leq 1$$

Note: Above method is good to learn for Math 280!

↑  
Travels from  $(-1, 3)$  to  $(3, -2)$ .

OR

$$\text{Slope of segment is } m = \frac{-2 - 3}{3 - (-1)} = \frac{-5}{4}.$$

Segment is on the line:

$$y - 3 = \frac{-5}{4}(x - (-1))$$

$$y = \frac{-5}{4}x + \frac{7}{4}$$

$$x = t, \quad y = \frac{-5}{4}t + \frac{7}{4}, \quad -1 \leq t \leq 3$$

Q: A bus driver was heading down a street in Walnut. He went right past a stop sign without stopping, went the wrong way on a one-way street, and then went on the left side of the road past a cop car. The cop did nothing, because he didn't break any traffic laws. Why not?