

Due date: \_\_\_\_\_

Name: \_\_\_\_\_

## Getting Ready for Derivatives (Part 5)

Notes

Recall the following trig identities:

$$\sin^2 x + \cos^2 x = 1$$

$$\sin(x + y) = \sin x \cos y + \cos x \sin y$$

$$\cos(x + y) = \cos x \cos y - \sin x \sin y$$

Also, recall that for logarithms and exponentials:

$$e^{\ln x} = \underline{\hspace{2cm}} \quad \text{and} \quad \ln e^x = \underline{\hspace{2cm}}$$

There's also the change of base formula for logarithms:

$$\log_b a = \frac{\log_c a}{\log_c b}$$

For example, this allows us to convert from any base to natural logarithms:  $\log_b a = \frac{\ln a}{\ln b}$ Lastly, it's time to memorize the definitions of  $\sinh x$  and  $\cosh x$ :

$$\sinh x = \underline{\hspace{2cm}}$$

$$\cosh x = \underline{\hspace{2cm}}$$

Notesex: Rewrite  $\cos(\sin^{-1} x)$  as an algebraic expression.

1. Rewrite  $\sin(\cos^{-1} x)$  as an algebraic expression.

2. Rewrite  $\tan(\sin^{-1} x)$  as an algebraic expression.

**Practice at home**

3. Try to fill in the following from memory.

a)  $\sin^2 x + \cos^2 x = \underline{\hspace{2cm}}$

b)  $\sin(x + y) = \underline{\hspace{4cm}}$

c)  $\cos(x + y) = \underline{\hspace{4cm}}$

d)  $e^{\ln x} = \underline{\hspace{2cm}}$

e)  $\ln e^x = \underline{\hspace{2cm}}$

f)  $\log_b a = \underline{\hspace{2cm}}$  (Change of base formula)

g)  $\sinh x = \underline{\hspace{2cm}}$  (Definition of  $\sinh x$ )

h)  $\cosh x = \underline{\hspace{2cm}}$  (Definition of  $\cosh x$ )

4. Rewrite  $\sin(\tan^{-1} x)$  as an algebraic expression.

5. Rewrite  $\cos(\sin^{-1} x)$  as an algebraic expression.