

4. Find the area of the largest rectangle that can be inscribed in the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$.

5. If you send a package via USPS Express Mail International, the length (the longest dimension) plus the girth (distance around thickest part) can't be more than 79 inches. What's the largest possible volume of a rectangular box with a square base that can be sent by USPS Express Mail International? And what are the dimensions of the box?

6. A right circular cylinder is inscribed in a cone with height h and base radius r . Find the largest possible volume of such a cylinder.

7. Find the volume of the largest right circular cone that can be inscribed in a sphere of radius 3.

8. An open box with a square base is going to be made. The sides of the box will cost \$3 per square foot, and the base will cost \$5 per square foot. What are the dimensions of the box with the largest volume that can be constructed for \$60?

9. Find the most general antiderivative for each of the following functions.

a) $f(x) = 8\sqrt[3]{x} - \frac{2}{x} + x^{9999} - \frac{10}{\sqrt{x}} + \frac{1}{x^3} + x\sqrt{x}$

b) $f(x) = \sin 3x + 2 \sec x \tan x - e^{-x} + 3^x + 19$

c) $f(x) = \frac{2}{1+x^2} - \frac{3}{\sqrt{1-x^2}} - \csc^2 x$

10. A particle is moving with the given data. Find the position of the particle.

$$a(t) = 3 \cos t - 2 \sin t, s(0) = 0, v(0) = 4$$

11. A particle is moving with the given data. Find the position of the particle.

$$a(t) = t^2 - 4t + 6, s(0) = 0, s(1) = 20$$

12. Find f if $f''(x) = 2e^x + 3 \sin x$, $f(0) = 0$, and $f(\pi) = 0$.

13. Estimate the area under the graph of $f(x) = \sqrt{x}$ between $x = 0$ and $x = 4$ using...

a) ...a lower sum with four rectangles of equal width.

b) ...an upper sum with four rectangles of equal width.

c) ...midpoints with four rectangles of equal width.

14. Estimate the area under the graph of $f(x) = e^{-x} + 1$ between $x = -1$ and $x = 1$ using...

a) ...right endpoints with four rectangles of equal width.

b) ...left endpoints with four rectangles of equal width.

c) ...midpoints with four rectangles of equal width.

15. Estimate the distance traveled in 12 hours given the following sample velocities...

Time (hours)	0	2	4	6	8	10	12
Velocity (mph)	60	63	64	50	45	48	70

a) ...using left-endpoint values.

b) ...using right-endpoint values.

16. Evaluate the following integrals using Riemann sums with right endpoints.

a) $\int_0^3 (2x + x^2) dx$

b) $\int_0^4 (x^2 - 4x + 2) dx$

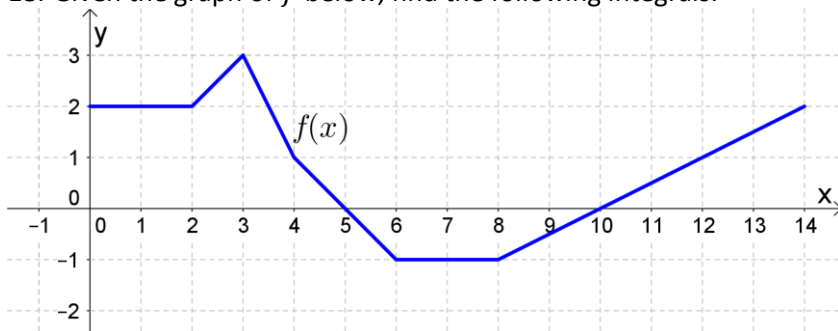
17. Suppose that $\int_1^5 f(x) dx = -2$, $\int_7^1 f(x) dx = 10$, and $\int_1^5 g(x) dx = 3$. Find the following.

a) $\int_5^1 3f(x) dx$

b) $\int_1^5 [g(x) - 4f(x)] dx$

c) $\int_5^7 f(x) dx$

18. Given the graph of f below, find the following integrals.



a) $\int_0^1 f(x) dx$

b) $\int_0^3 f(x) dx$

c) $\int_3^6 f(x) dx$

d) $\int_4^6 f(x) dx$

e) $\int_4^{10} f(x) dx$

f) $\int_0^{14} f(x) dx$

19. Graph the following integrands and use the area under the graph to evaluate the integral.

a) $\int_{-1}^6 (|x - 3| + 1) dx$

b) $\int_0^2 (3 + \sqrt{4 - x^2}) dx$

20. Use Part 1 of the Fundamental Theorem of Calculus to find the derivative of the following functions.

a) $f(x) = \int_3^{1/x} \sin^5 t dt$

b) $g(x) = \int_x^3 (t^2 - 5)^{10} dt$

c) $h(x) = \int_{\sqrt{x}}^{2x} \tan^{-1} t dt$

21. Evaluate the following integrals.

a) $\int_4^9 (2x\sqrt{x} - 3) dx$

b) $\int_0^{\pi/8} \sin 2x dx$

c) $\int_{\pi/6}^{\pi/2} \csc^2 x dx$

d) $\int_0^1 \frac{5}{1+x^2} dx$

e) $\int_0^{\pi/3} (2x - \sec x \tan x) dx$

f) $\int_{1/2}^1 \frac{1}{2x} dx$

g) $\int_0^1 e^{3x} dx$

h) $\int_0^7 \frac{1}{\sqrt[3]{x+1}} dx$

i) $\int \frac{4x^2+2}{(2x^3+3x)^4} dx$

j) $\int e^{2 \cos x} \cdot \sin x dx$

k) $\int 3xe^{x^2+2} dx$

l) $\int x^2 e^{-2x} dx$

m) $\int x^2 \ln x dx$

n) $\int e^{2x} \cos x dx$

o) $\int x\sqrt{2x+1} dx$

p) $\int_e^{e^2} \frac{(\ln x)^3}{2x} dx$

q) $\int_0^{\pi/2} (7^{\cos x} \sin x) dx$

r) $\int_0^1 \tan^{-1} x \, dx$

s) $\int_{-3}^3 |x| \tan x \, dx$

22. Suppose the velocity function of a particle is $v(t) = t^2 - 2t$ (in meters per second). Find the distance traveled by the particle during the time period $-2 \leq t \leq 5$.