

Test #3 (Part 1, No Calculator)

Name: _____

Math 160, Prof. Beydler

Thursday, November 29, 2018

Directions: Show all work. No calculator, books, or notes. Your desk and lap must be clear (no phones, no smart watches, etc.). If you have a phone in your lap or on your chair, it is considered cheating, and you will receive a zero on this test. Write your answers in the indicated places, or box your answers. When you're finished with Part 1, please turn it in, take a bathroom break, get your calculator out, and start Part 2. Good luck!

1. (1 point) Are $\langle -2, -3 \rangle$ and $\langle -6, 4 \rangle$ orthogonal?

$$(-2)(-6) + (-3)(4) = 0$$

orthogonal not orthogonal (circle one)

2. (4 points) Determine whether the equation represents a parabola, an ellipse, or a hyperbola. If the graph is a parabola, find the vertex, focus, directrix, and focal diameter. If it is an ellipse, find the center, foci, vertices, lengths of the major and minor axes, and eccentricity. If it is a hyperbola, find the center, foci, vertices, and asymptotes. Then sketch the graph of the equation. (Note: $\sqrt{2} \approx 1.4$ and $\sqrt{6} \approx 2.4$)

$4x^2 - 2y^2 = 8$ parabola ellipse **hyperbola** (circle one)

$$\frac{x^2}{2} - \frac{y^2}{4} = 1$$

\uparrow \uparrow
 $\pm\sqrt{2}$ in ± 2 in
 x -dir. y -dir.

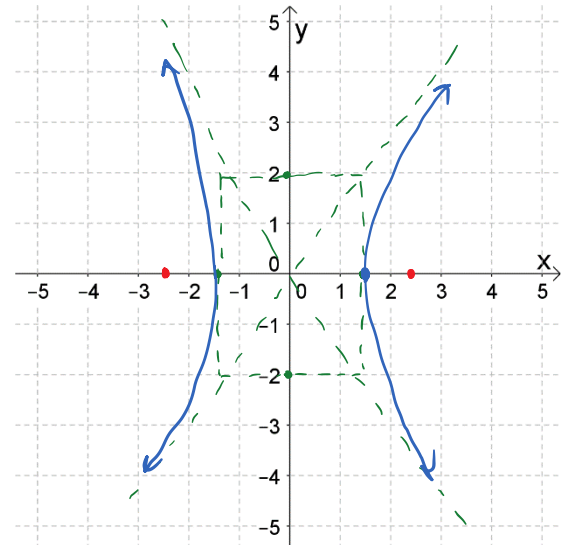
Center: $(0, 0)$

$$c = \sqrt{2+4} = \sqrt{6}$$

Foci: $(\pm\sqrt{6}, 0)$

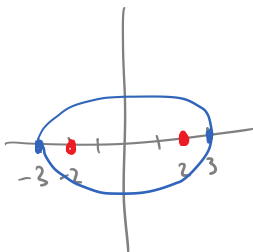
Vertices: $(\pm\sqrt{2}, 0)$

Asymptotes: $y = \pm\frac{2}{\sqrt{2}}x$



3. (2 points) Find an equation for the ellipse that satisfies the given conditions.

Foci: $(\pm 2, 0)$, vertices: $(\pm 3, 0)$



$$\frac{x^2}{9} + \frac{y^2}{5} = 1$$

\uparrow
 3^2

Answer: $\frac{x^2}{9} + \frac{y^2}{5} = 1$

$$c = \sqrt{a^2 - b^2}$$

$$2 = \sqrt{9 - b^2}$$

$$4 = 9 - b^2$$

$$b^2 = 5$$

4. (4 points) Determine whether the equation represents a parabola, an ellipse, or a hyperbola. If the graph is a parabola, find the vertex, focus, directrix, and focal diameter. If it is an ellipse, find the center, foci, vertices, lengths of the major and minor axes, and eccentricity. If it is a hyperbola, find the center, foci, vertices, and asymptotes. Then sketch the graph of the equation.

$$x^2 + 4x = 4y - 4$$

parabola ellipse hyperbola (circle one)

$$x^2 + 4x + 4 = 4y - 4 + 4$$

$$(x+2)^2 = 4y$$

$$\text{Vertex: } (-2, 0)$$

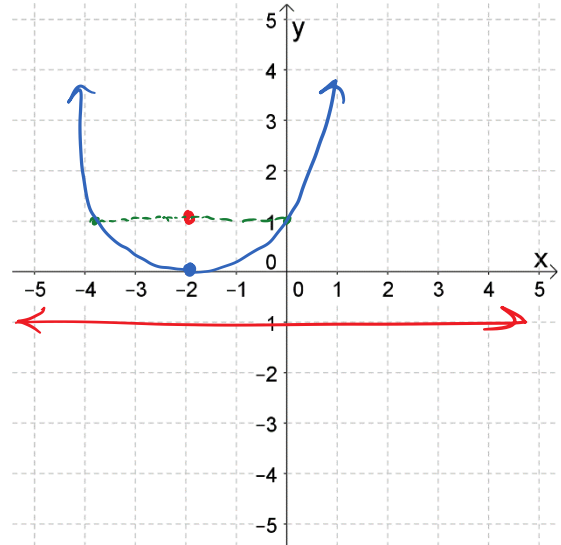
$$4p = 4$$

$$p = 1$$

$$\text{Focus: } (-2, 1)$$

$$\text{Directrix: } y = -1$$

$$\text{Focal diameter: } |4p| = |4| = 4$$



5. (3 points) Find all solutions to the system:
$$\begin{cases} x^2 - y^2 = 1 \\ 2x^2 - y^2 = x + 3 \end{cases}$$

Answer: $(-1, 0), (2, \sqrt{3}), (2, -\sqrt{3})$

$$\begin{array}{r} x^2 - y^2 = 1 \\ - (2x^2 - y^2 = x + 3) \\ \hline \end{array}$$

$$-x^2 = -x - 2$$

$$x^2 - x - 2 = 0$$

$$(x+1)(x-2) = 0$$

$$\begin{array}{cc} \downarrow & \downarrow \\ x = -1 & x = 2 \end{array}$$

$$(-1)^2 - y^2 = 1$$

$$y^2 = 0$$

$$y = 0$$

$$(2)^2 - y^2 = 1$$

$$y^2 = 3$$

$$y = \pm\sqrt{3}$$